

Perspectives for high-precision $\alpha_S(m_Z^2)$ determinations from future e^+e^- measurements at the FCC-ee

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Thematic Areas:

- (EF01) EW Physics: Higgs Boson properties and couplings
- (EF02) EW Physics: Higgs Boson as a portal to new physics
- (EF03) EW Physics: Heavy flavor and top quark physics
- (EF04) EW Physics: EW Precision Physics and constraining new physics
- (EF05) QCD and strong interactions: Precision QCD
- (EF06) QCD and strong interactions: Hadronic structure and forward QCD
- (EF07) QCD and strong interactions: Heavy Ions
- (EF08) BSM: Model specific explorations
- (EF09) BSM: More general explorations
- (EF10) BSM: Dark Matter at colliders

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The large amount of data expected to be recorded in e^+e^- collisions at the Future Circular Collider (FCC-ee) [1, 2] will offer multiple possibilities for unprecedented determinations of the strong coupling constant, $\alpha_S(m_Z^2)$, with per-mil uncertainties [3, 4, 5]. The experimental studies of hadronic observables, such as the R ratio [6, 7], tau decays [8, 9, 10]; Z and W decays [11, 12]; event shapes [13, 14, 15], and jet rates [16, 17]; hard [18, 19] and soft [20, 21] parton-to-hadron fragmentation functions; and the photon structure function $F_2^\gamma(x, Q^2)$ via photon-photon interactions [22], among others; combined with their careful analysis with the corresponding state-of-the-art perturbative QCD calculations, will provide accurate and precise $\alpha_S(m_Z^2)$ determinations.

The FCC-ee will deliver unparalleled samples of $5 \cdot 10^8$ W bosons and $3 \cdot 10^{12}$ Z bosons, decaying hadronically, in e^+e^- collisions at the Z pole ($\sqrt{s} \approx 91$ GeV) and WW threshold ($\sqrt{s} \approx 160$ GeV), respectively. The corresponding high-precision measurements of hadronic W and Z pseudo-observables (total widths, $\Gamma_{W,Z}$; ratio of hadronic-to-leptonic widths, R_ℓ ; and peak hadronic cross section at the Z pole, σ_Z^{had}) will allow the extraction of the QCD coupling constant $\alpha_S(m_Z^2)$ with uncertainties below the 0.2% level [3, 12, 11] in a few different ways. With challengingly small statistical uncertainties, and accounting for the expected progress in the computation of theoretical higher-order N⁴LO QCD $\mathcal{O}(\alpha_S^5)$, $\mathcal{O}(\alpha^2, \alpha^3)$ electroweak, and mixed QCD \oplus EW $\mathcal{O}(\alpha\alpha_S^2, \alpha\alpha_S^3, \alpha^2\alpha_S)$ corrections missing today, the leading propagated uncertainties on $\alpha_S(m_Z^2)$ will be of experimental systematic nature. The improvements on the detector design expected in order to match the systematic and statistical precision on Γ_Z , R_ℓ , and σ_Z^{had} [1] will be studied in order to determine the ultimate uncertainty eventually reachable in those $\alpha_S(m_Z^2)$ extractions at the FCC-ee.

For all extractions not depending on hadronic resonance (τ , Z, W) decays, measurements as a function of the invariant mass of the final hadronic system offer a self-normalized determination based on the QCD evolution equations. In this context, one can exploit the $3 \cdot 10^8$ e^+e^- hadronic events expected in the Higgs and top-quark operation runs at $\sqrt{s} \approx 240$ and 365 GeV, respectively. For analyses at lower energies than the Z pole, two specific possibilities have been considered in [23]. The first one is to organize data-taking from $\sqrt{s} \approx 30$ to 90 GeV center-of-mass energies, in such a way so as to record 10^9 $e^+e^- \rightarrow$ hadrons events at several intermediate energies. The second one consists in using the $e^+e^- \rightarrow \gamma +$ hadrons events with initial-state radiation (ISR) recorded from the foreseen data taking at and around the Z pole. The importance of detector design will be evaluated in particular regarding: i) the overall angular and momentum acceptance of the detector for hadrons, ISR, and (where relevant) scattered beam e^\pm ; ii) the performance for flavoured (b/c /light-quark/gluon) jets reconstruction and corresponding mistagging probabilities; iii) the availability of light charged hadron ($\pi/K/p$) identification. The resulting detector requirements will be spelled out. The opportunities brought in by dedicated intermediate-energy runs for improving the detector calibration and checking the event simulations will be also investigated. This study might result in a more detailed FCC-ee running proposal.

For all methods above, theoretical developments are required in order to match the expected experimental precision, including computation of higher-order (both fixed-order and resummed log) QCD corrections, and non-perturbative QCD effects (hadronization, power-suppressed terms, hadron masses, etc.). The exploitation of modern jet substructure techniques to potentially improve the $\alpha_S(m_Z^2)$ determinations will be also considered and evaluated.

References

- [1] FCC collaboration, A. Abada et al., *FCC-ee: The Lepton Collider: Future Circular Collider Conceptual Design Report Volume 2*, *Eur. Phys. J. ST* **228** (2019) 261–623.
- [2] FCC collaboration, A. Abada et al., *FCC Physics Opportunities: Future Circular Collider Conceptual Design Report Volume 1*, *Eur. Phys. J. C* **79** (2019) 474.
- [3] TLEP DESIGN STUDY collaboration, M. Bicer et al., *First Look at the Physics Case of TLEP*, *JHEP* **01** (2014) 164, [[1308.6176](#)].
- [4] D. d’Enterria and P. Z. Skands, eds., *Proceedings, High-Precision α_s Measurements from LHC to FCC-ee: Geneva, Switzerland, October 2-13, 2015*, (Geneva), CERN, 2015.
- [5] D. d’Enterria and S. Kluth, eds., *$\alpha_s(2019)$: Precision measurements of the QCD coupling*, vol. ALPHAS2019, SISSA, 2019.
- [6] A. Nesterenko, *Electron–positron annihilation into hadrons at the higher-loop levels*, *Eur. Phys. J. C* **77** (2017) 844, [[1707.00668](#)].
- [7] D. Boito, M. Golterman, A. Keshavarzi, K. Maltman, D. Nomura, S. Peris et al., *Strong coupling from $e^+e^- \rightarrow$ hadrons below charm*, *Phys. Rev. D* **98** (2018) 074030, [[1805.08176](#)].
- [8] D. Boito, M. Golterman, K. Maltman, J. Osborne and S. Peris, *Strong coupling from the revised ALEPH data for hadronic τ decays*, *Phys. Rev. D* **91** (2015) 034003, [[1410.3528](#)].
- [9] A. Pich and A. Rodríguez-Sánchez, *Determination of the QCD coupling from ALEPH τ decay data*, *Phys. Rev. D* **94** (2016) 034027, [[1605.06830](#)].
- [10] D. Boito, M. Golterman, K. Maltman and S. Peris, *Strong coupling from hadronic τ decays: A critical appraisal*, *Phys. Rev. D* **95** (2017) 034024, [[1611.03457](#)].
- [11] D. d’Enterria and V. Jacobsen, *Improved strong coupling determinations from hadronic decays of electroweak bosons at N^3LO accuracy*, [2005.04545](#).
- [12] D. d’Enterria and M. Srebre, *α_s and V_{cs} determination, and CKM unitarity test, from W decays at NNLO*, *Phys. Lett. B* **763** (2016) 465–471, [[1603.06501](#)].
- [13] A. Banfi, H. McAslan, P. F. Monni and G. Zanderighi, *A general method for the resummation of event-shape distributions in e^+e^- annihilation*, *JHEP* **05** (2015) 102, [[1412.2126](#)].
- [14] A. Kardos, G. Somogyi and Z. Trócsányi, *Soft-drop event shapes in electron–positron annihilation at next-to-next-to-leading order accuracy*, *Phys. Lett. B* **786** (2018) 313–318, [[1807.11472](#)].
- [15] A. Kardos, S. Kluth, G. Somogyi, Z. Tulipánt and A. Verbytskyi, *Precise determination of $\alpha_s(M_Z)$ from a global fit of energy–energy correlation to NNLO+NNLL predictions*, *Eur. Phys. J. C* **78** (2018) 498, [[1804.09146](#)].
- [16] A. Banfi, H. McAslan, P. F. Monni and G. Zanderighi, *The two-jet rate in e^+e^- at next-to-next-to-leading-logarithmic order*, *Phys. Rev. Lett.* **117** (2016) 172001, [[1607.03111](#)].
- [17] A. Verbytskyi, A. Banfi, A. Kardos, P. F. Monni, S. Kluth, G. Somogyi et al., *High precision determination of α_s from a global fit of jet rates*, *JHEP* **08** (2019) 129, [[1902.08158](#)].
- [18] B. A. Kniehl, G. Kramer and B. Potter, *Strong coupling constant from scaling violations in fragmentation functions*, *Phys. Rev. Lett.* **85** (2000) 5288–5291, [[hep-ph/0003297](#)].
- [19] P. Bolzoni, B. Kniehl and A. Kotikov, *Gluon and quark jet multiplicities at $N^3LO+NNLL$* , *Phys. Rev. Lett.* **109** (2012) 242002, [[1209.5914](#)].
- [20] R. Perez-Ramos and D. d’Enterria, *Energy evolution of the moments of the hadron distribution in QCD jets including NNLL resummation and NLO running-coupling corrections*, *JHEP* **08** (2014) 068, [[1310.8534](#)].

- [21] D. d’Enterria and R. Pérez-Ramos, α_s determination at NNLO*+NNLL accuracy from the energy evolution of jet fragmentation functions at low z , in *50th Rencontres de Moriond on QCD and High Energy Interactions*, p. 117, 5, 2015. [1505.02624](#).
- [22] S. Albino, M. Klasen and S. Soldner-Rembold, *Strong Coupling Constant from the Photon Structure Function*, *Phys. Rev. Lett.* **89** (2002) 122004, [[hep-ph/0205069](#)].
- [23] Andrii Verbytskyi, “Perspective of the α_s extraction from the FCC data.” Talk given at the 3rd FCC Physics and Experiments Workshop https://indico.cern.ch/event/838435/contributions/3635706/attachments/1969408/3275588/Genf2020_Andrii_Verbytskyi.pdf, January, 2020.