

# Electroweak parton distributions and fragmentations at ultrahigh energies

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At energy scales well above the electroweak (EW) scale ( $M_{W,Z}$ ), all Standard Model (SM) particles are essentially massless and should be viewed as EW partons, collinearly radiated off the high-energy leptonic beams. In a recent publication [1], we studied the physics cases at a future high energy muon collider and argued that it is appropriate to adopt the EW partonic picture for inclusive processes, a notion thus far only reserved for hadron colliders. We set up the Dokshitzer-Gribov-Lipatov-Altarelli-Parisi (DGLAP) formalism and calculated the EW parton luminosities. We presented cross sections for some important SM processes for a proposed muon collider. Yet, there are theoretical and practical issues that we must continue to tackle.

**Matching.** When the collision energy is far above the threshold ( $\hat{s} \gg 4m^2$ ), the EW parton distribution functions (PDF) formalism is appropriate to predict the (semi-)inclusive cross sections. However, when the energy is right above threshold ( $\hat{s} \geq 4m^2$ ), the factorization picture suffers from large corrections due to the threshold constraint of massive particles. Instead, we expect the diagrammatic calculations at a fixed order (FO) is valid in this regime, analogous to the fixed-flavor-number (FFN) scheme to treat the heavy-flavor production. The transition from the low- to high-energy regimes requires a systematical matching between the FO diagrammatic calculation and the PDF resummation.

**Fragmentation.** We have not taken into account the effects of the final-state radiation (FSR) in Ref. [1]. At very high energy, the dominant FSR features can be described by the “fragmentation functions” [2, 3], which effectively resums the large logarithms due to FSR collinear enhancement. This FSR resummation can be performed in terms of parton showering algorithms [2], which evolves according to the Sudakov form factor. Around the threshold region, a similar matching to the FO calculation is also needed to capture the massive particle effects.

**Hadronic colliders.** In Ref. [1], we took  $\mu^+\mu^-$  as an example of the leptonic collisions to demonstrate the EW PDF formalism. It is straightforward to apply this formalism to the high-energy hadronic colliders. The complication lies that we need to run the QCD as well as the EW gauge groups simultaneously, which involves 60 PDFs in the isospin ( $\mathbf{T}$ ) and charge-parity (CP) basis [4]. The photon PDF of a proton at a low scale is more subtle [5]. Furthermore, different from the leptonic case, we can have a significant contribution to the EW PDFs from the proton structure functions even at the starting scale of the evolution ( $\mu \sim M_{W,Z}$ ) [6]. We would like to see the implications of the EW PDFs to phenomenological

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predictions at the FCC-hh collider.

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